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WEBSE_{IDF}: A Web-Based System for the Estimation of IDF Curves in Central Chile

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Abstract: The lack of reliable continuous rainfall records can exacerbate the negative impact of extreme storm events. The inability to describe the continuous characteristics of rainfall from storm events increases the likelihood that the design of hydraulic structures will be inadequate. To mitigate extreme storm impacts and improve water governance at the catchment scale, it is vital to improve the availability of data and the array of tools used to model and forecast hydrological processes. In this paper, we describe and discuss the implementation of a web-based system for the estimation of intensity–duration–frequency (IDF) curves (WEBSE_{IDF}) in Chile. The web platform was constructed using records from 47 pluviographic gauges available in central Chile (30–40° S), with at least 15 years of reliable records. IDF curves can be generated for durations ranging from 15 min to 24 h. In addition, the extrapolation of rainfall intensity from pluviograph to pluviometric gauges (i.e., 24-h rainfall accumulation) can be carried out using the storm index (S_I) method. IDF curves can also be generated for any spatial location within central Chile using the ordinary Kriging method. These procedures allow the generation of numerical and graphical displays of IDF curves, for any selected spatial location, and for any combination of probability distribution function (PDF), parameter estimation method, and type of IDF model. One of the major advantages of WEBSE_{IDF} is the flexibility of its database, which can be easily modified and saved to generate IDF curves under user-defined scenarios, that is, changing climate conditions. The implementation and validation of WEBSE_{IDF} serves as a decision support system, providing an important tool for improving the ability of the Chilean government to mitigate the impact of extreme hydrologic events in central Chile. The system is freely available for students, researchers, and other relevant professionals, to improve technical decisions of public and private institutions.

Keywords: extreme storm events; rainfall intensity; IDF curves; IDF model; web-based system

1. Introduction

Intensity–duration–frequency (IDF) curves are constructed based on the frequency of annual maximum rainfall intensities. They are an essential tool for the design of drainage and flood prevention infrastructures in urban areas. IDF curves ensure that hydraulic structures are adequate for, and can

withstand the impacts of, extreme storm events, that is, that the collapse of drainage systems, damage to infrastructure, and loss of human life will not occur as the result of large floods, landslides, mudflows, and so on [1–3]. Extremes in the variability of the hydrologic cycle increase the negative effects of major storm events, because infrastructure design is less likely to be commensurate to the hydrologic effects of these storms [4,5]. Recent studies have used IDF curves to force hydrological models evaluating river basin responses for hydrologic design and water management [6–9].

As the probability of observing a greater frequency and intensity of storm events is expected to increase [10,11], the development of IDF curves will be a crucial challenge to minimize the vulnerability and exposure of ecosystems and human systems to the effects of global warming [12–16]. Research efforts have been focused on developing and evaluating IDF curves under non-stationary conditions (climate change scenarios), in order to establish differences between historical and future design storms [17–21]. However, in many places of the world, the inability to access data to evaluate mitigation and adaption options, and the lack of technical resources to implement adaptation options, have been identified as barriers to climate change adaptation [22,23]. The lack of consistent spatio-temporal distribution of ground-based rainfall intensity records is an additional challenge that governments and water resources managers face. To address this gap, web-based systems are a supportive tool aimed to storing and displaying historical and future projections of storm designs.

Central Chile (30–40° S), where 73% of the national population is concentrated [24], is cyclically impacted by extreme hydrological events. Precipitation along this Mediterranean territory is caused primarily by winter (austral) frontal systems [25–29]. These systems generate storms that can be similar in intensity to the convective systems registered in northern Chile [30]. It is estimated that the Chilean Government invested about US\$1.5M to help with the recovery efforts derived from the damage caused by frontal precipitation systems that affected central Chile between 2000 and 2009 [31]. This magnitude of damages can be attributed to the lack of spatio-temporal hydrological information, the unplanned development activities by private and public entities, and the poor implementation of suitable policies for land management. In other words, the region is not well prepared to face the extreme events resulting from global warming [16].

Given the Chilean authorities' interest on implementing a statistically reliable and robust system to store historic records of extreme storm events for central Chile, a web-based system for the generation of IDF curves (WEBSE_{IDF}) was developed using rainfall intensity records from 47 pluviograph stations distributed in central Chile. WEBSE_{IDF} makes it possible to construct IDF curves for durations of 0.25, 0.5, 0.75, 1, 4, 6, 12, and 24 h. The system also enables the extrapolation of IDF curves to ungauged areas, that is, in pluviometric gauges, IDF curves can be constructed using the storm index (S_I) method, a linear scaling method proposed by the authors of [32]. A geostatistical method to extrapolate IDF curves has been also included in WEBSE_{IDF}, that is, the ordinary Kriging method. This system provides a solution for ungauged areas that require the development of IDF curves for hydraulic structure design. Details about the structure and use of WEBSE_{IDF} are provided in the following sections of this manuscript.

2. Methods

In this section, the procedures that were used to construct the IDF curves and their further integration into WEBSE_{IDF} are described. Each of the sections that comprise the methodology is linked to the process of developing the database and the elements (user's interface) that allow the user to interact with the tools in WEBSE_{IDF}.

2.1. Intensity–Duration–Frequency Relationship

Precipitation, as a component of the water cycle, can be characterized based on three fundamental relationships: (1) the intensity, or temporal rate of precipitation (mm/h); (2) the duration for which the given average rainfall intensity will occur; and (3) the return period (T), which is the frequency or probability of occurrence [32–34]. The procedure to construct IDF curves is conducted by fitting

rainfall intensity records to a probability density function (PDF), or a cumulative distribution function (CDF), while accounting for a specific duration that can vary from 15 min up to 24 h, as desired [34]. Annual maximum series (AMS) or partial duration series (PDS) can be used to construct the IDF Curves [19,35]. The maximum rainfall intensity for each duration is related to a return period (T), corresponding to a CDF. In terms of probability, T can be defined as a function of the probability of exceedance (occurrence) as follows:

$$P(X > x_T) = \frac{1}{T} \text{ and } P(X \leq x_T) = 1 - \frac{1}{T}$$

where,

- $P(X > x_T)$ is the probability of exceedance within a year of a storm event with rainfall intensity x_T .
- $P(X \leq x_T)$ is the probability of occurrence within a year of a storm event with rainfall intensity x_T .
- T is the return period or the number of years.

If the CDF is known, the frequency of extreme storms can be determined by fitting annual maximum rainfall intensity records to a PDF that best describes the temporal distribution of these independent events. According to the authors of [36], among all available PDFs, the most commonly used functions for describing random variables for maximum rainfall intensities are the following: generalized extreme value (GEV), Gumbel, and Pearson type-III. In WEBSE_{IDF}, the user has the option to select some of the aforementioned PDFs to fit the historical intensity records, while accounting for different “goodness of fit” tests. Although this flexibility is available, it has been shown by the authors of [30] that the fit of the Gumbel distribution obtains good results in central Chile, where most pluviograph gauges are concentrated. Likewise, the Pearson-III PDF has demonstrated a good fit for data on arid and semi-arid regions of Chile (29–32° S), where rainfall intensity records have higher variability.

2.2. Probability Density Functions Included in WEBSE_{IDF}

When annual maximum rainfall records are available, a frequency analysis can be conducted to estimate the exceedance probabilities, whose reciprocal is the return period [34–36]. Table 1 summarizes the PDFs implemented in WEBSE_{IDF}. Further details related to the theory of frequency analysis in hydrology can be found in the literature [37–42]. The available PDFs in the WEBSE_{IDF} system are considered sufficient for most modeling situations.

Table 1. Probability density functions available in web-based system for the estimation of intensity–duration–frequency (IDF) curves (WEBSE_{IDF}).

| Name | Probability Density Function |
|---------------------------------|---|
| Generalized Extreme Value (GEV) | $F(X) = \exp \left[- \left(1 - k \frac{x - \mu}{\alpha} \right)^{\frac{1}{k}} \right]$ <ul style="list-style-type: none"> • where k is the shape parameter • if $k = 0$, is Type I or Gumbel • if $k < 0$, not considered in this study see [31] • if $k > 0$, is Type III or Weibull |
| Gumbel | $F(X) = e^{-e^{-\alpha (x - \mu)}}$ <ul style="list-style-type: none"> • where α and μ are the scale and location parameters of the distribution |
| Pearson Type-III | $F(X) = \frac{1}{\alpha \Gamma(\beta)} \int_0^x e^{-\left(\frac{x-\mu}{\delta}\right)} \left(\frac{x-\mu}{\delta}\right)^{\beta-1} dx$ <ul style="list-style-type: none"> • where α, δ and μ are the parameters of the distribution |

2.3. Parameter Estimation Methods

In hydrology, PDF parameters are usually estimated using the method of moments (MoM), which is simple and easy to implement. The maximum likelihood (ML) method is more complex due to the required algebraic manipulation [43,44], even though it can be very efficient when the sample size is large [45]. Greenwood [46] proposed another method to estimate parameters using probability weighted moments (PWM). One advantage of this method is that it can be written in an inverse form for Gumbel and Weibull; it also provides better results for the GEV in terms of bias and variance for sample sizes between 15 and 100 data points [44,47]. These advantages outweigh the fact that for small sample sizes, the ML can generate spurious values for the k parameter [48]. These three methods—MoM, ML, and PWM—have been implemented in WEBSE_{IDF} and allow the user to compare the performance and results provided by the methods.

2.4. Mathematical Modelling of IDF Curves

Traditionally, IDF curves are represented graphically, which can introduce bias during the reading of a desired IDF curve. Interpretation errors are generally associated with the resolution of the printed curve on paper, and this error is amplified when the information is used for the design of hydraulic structures. Bernard [49] was one of the first to develop a mathematical model that describes rainfall intensity as a function of certain return period (T) and duration (D). This model is parametrized by simple linear regression and can produce a family of IDF curves, eliminating subjective reading errors. Currently, there is a large range of mathematical models for the generation of IDF curves, all with a similar structure to that of Bernard's model [49]. The mathematical models for IDF curve estimation that are available in WEBSE_{IDF} are listed on Table 2; while not exhaustive, they are considered sufficient for most modeling scenarios.

Table 2. Mathematical models for IDF curve estimation available in WEBSE_{IDF}.

| Author | Model |
|----------------------------------|---|
| Sherman (1931) [50] | $i = \frac{kT^m}{(D+b)^n}$ |
| Bernard (1932) [49] | $i = \frac{kT^m}{D^n}$ |
| Wenzel (1982) [51] | $i = \frac{k}{D^n+b}$ |
| Chen (1983) [52] | $i = i_1^T \frac{k}{(D+b)^n}$ |
| Chow et al. (1988) [43] | $i = \frac{kT^m}{D^n+b}$ |
| Koutsoyiannis et al. (1998) [37] | $i = k \left[\frac{m - \ln[-\ln(1 - \frac{1}{T})]}{(D+b)^n} \right]$ |

k, b, m, n are parameters of the IDF models.

2.5. Goodness-of-Fit of PDFs and Mathematical Models

To verify the consistency between the rainfall records, the PDFs, and the IDF models, three goodness-of-fit tests are used: (1) the Mann–Whitney U test can be applied with the aim of determining if the two independent samples (observed and modeled rainfall intensity) come from the same population [53]; (2) the non-parametric Kolmogorov–Smirnov (K–S) test [54], which is important to determine the maximum deviation (theoretic and observed) of the modeled rainfall intensity; and (3) the coefficient of determination (R^2), which is used to estimate the percentage of variance explained by the modeled rainfall intensity [55], which can be determined as a combination of any selected PDF and/or IDF model. Both the Mann–Whitney U and K–S tests can be evaluated by looking at their p -values under the module Statistics (see Section 3.4). In the K–S test, the null hypothesis regarding the distribution of rainfall intensity records is rejected if the test statistic, D (maximum difference between

observed and estimated rainfall intensity), is greater than the critical value obtained from a table associated to a desired alpha value (see Table 1). The Mann–Whitney test is based on a comparison between each observation and each value estimated by the fitted PDF. If both series have the same median, then each observed rainfall value has an equal probability of being greater or smaller than each value estimated by the PDF. As it is also possible that two or more observations estimated from the PDF can be equal to the observed rainfall intensity value, U can be calculated by allocating half of the tie to the observed rainfall intensity records, and the other half to the estimated values. This can be done by using the normal approximation with an adjustment to the standard deviation (see Table 1). It is important to mention that all tests are calculated by comparing the rainfall intensity records of both observed and theoretical distributions for all durations and period returns (two column vectors). A summary of the three goodness-of-fit tests implemented in WEBSE_{IDF} is presented in Table 3.

Table 3. Goodness-of-fit tests used in WEBSE_{IDF}.

| Goodness-of-Fit Test | Reference Equation | Parameters |
|--|---|---|
| Kolmogorov–Smirnov Test | $D = \sup F_n(x_i) - F(x_i) $ If $D \leq D_t \rightarrow p\text{-value} \geq \alpha\text{-level}$: accept H_0 If $D > D_t \rightarrow p\text{-value} < \alpha\text{-level}$: reject H_0 | <ul style="list-style-type: none"> • $F_n(x_i)$ observed frequency of rainfall intensity • $F(x_i)$ theoretical frequency of rainfall intensity • H_0 both the observed and theoretical frequencies have the same cumulative distribution function (CDF) • H_1 both the observed and theoretical frequencies have a different cumulative distribution function (CDF) • D_t is the absolute maximum distance (supremum) between the CDFs of both populations |
| Coefficient of Determination (R^2) | $R^2 = 1 - \frac{\sum (y_i - \hat{y}_i)^2}{\sum (y_i - \bar{y}_i)^2}$ | <ul style="list-style-type: none"> • y_i observed rainfall intensity or observed rainfall frequency. • \hat{y}_i modeled rainfall intensity, or theoretical rainfall frequency. • \bar{y}_i averaged observed rainfall intensity |
| Mann–Whitney U Test $n < 25$ | $Z = (n_1 \times n_2) + \left(\frac{n_1 + n_2 + 1}{2} \right) - \sum R_1$ | <ul style="list-style-type: none"> • n_1 sample size of group R_1 • n_2 sample size of group R_2 • $\sum R_1$ is the sum of ranges of group R_1 • $\sum R_2$ is the sum of ranges of group R_2 • H_0 the cumulative distributions functions of group R_1 and group R_2 are identical • H_1 the cumulative distributions functions of group R_1 and group R_2 are not identical. |
| Mann–Whitney U Test $n > 25$ | $Z = \frac{\sum R_1 - \sum R_2 - \left[(n_1 - n_2) \times \left(\frac{n_1 + n_2 + 1}{2} \right) \right]}{\sqrt{n_1 \times n_2 \times \left(\frac{n_1 + n_2 + 1}{3} \right)}}$ | |

2.6. Extrapolation and Interpolation of IDF Curves

Most of the rain gauges in Chile measure rainfall accumulation every 24 h, limiting the capacity to construct IDF curves in areas lacking pluviograph gauges or tipping buckets that can provide rainfall accumulation for durations shorter than 24 h. In order to extend the spatial distribution of IDF curves to pluviometric gauges (24-h rainfall accumulation), extrapolation or interpolation methods can be applied. Two methods have been implemented in WEBSE_{IDF}: (1) storm index; and (2) ordinary Kriging. Details about both methods are described below.

2.6.1. Storm Index Method

The storm index (S_I), proposed by the authors of [32], was implemented in WEBSE_{IDF}. S_I is a dimensionless scaling ratio that can be calculated for any pluviographic gauge. This ratio is calculated between the maximum rainfall intensity in 24 h and the rainfall intensity for all durations less or equal than 24 h. Pizarro et al. [32] indicated that reliable constructions of IDF curves in pluviometric gauges are attained when the maximum absolute difference between the raw rainfall intensity in 24 h for both pluviographic and pluviometric gauges does not exceed 2 mm/h. The method assumes that rainfall characteristics observed in the pluviographic gauge are similar to those of the pluviometric gauge;

however, this does not necessarily mean that the two gauges have to share similar climatic patterns. In fact, Pizarro et al. [30] concluded that maximum rainfall intensities values in Chile can be similar at different latitudes, that is, convective storms of northern Chile can be of similar intensity than frontal storms of central and southern Chile. The S_I method was developed by [1] and validated for central Chile by [32]. The S_I method is defined by the following expression:

$$S_{I(ij)} = \frac{I_{\max(ij)}}{I_{\max(24,j)}}$$

where $S_{I(ij)}$ is the storm index in the pluviograph gauge for the duration i (hours), and the return period j (years); $I_{\max(ij)}$ is the maximum rainfall intensity for the duration i and return period j ; and $I_{\max(24,j)}$ is the maximum rainfall intensity in 24 h for the return period j . This linear scaling method allows the increase of the spatial distribution of maximum rainfall intensity and the corresponding IDF curves, thus improving the availability of hydrological data for hydrologic design and water management. The WEBSE_{IDF} also makes this method available so the user can spatially extrapolate rainfall intensity data (and IDF curves) to pluviometric gauges.

2.6.2. Ordinary Kriging

Geostatistical interpolation was also implemented in WEBSE_{IDF}. Ordinary Kriging interpolation is used to reproduce a spatial prediction of rainfall intensity at any location of interest within the domain of interest. This method uses a semivariogram or a covariance model that relies on spatial relationships of rainfall intensity data [56,57]. The method is a geostatistical interpolation method similar to the inverse distance weighting (IDW) because it also weights nearby data points. In Kriging, however, the weights are not only dependent on distance; but they also depend on the overall spatial distribution of the data points. The method has been widely used in hydrology to determine spatio-temporal patterns of rainfall, and also in other environmental sciences [58–60]. The Kriging method is defined as a linear sum:

$$\hat{Z}(S_0) = \sum_{i=1}^N \lambda_i Z(S_i)$$

where,

- $Z(S_i)$ is the measured rainfall intensity value at the location i
- λ_i is the weight for the location i
- S_0 is the predicted location
- N is the number of measured values

2.7. Implementation and Validation of WEBSE_{IDF}

WEBSE_{IDF} offers a geographical information system (GIS) interface that enables users to easily access historical information from individual or multiple pluviograph gauges located in central Chile. Additionally, users provide updates to the database (in the necessary format) if newer data or gauges are needed to construct IDF curves. WEBSE_{IDF} is similar in structure and components to the web tool developed and described by the authors of [23], for the generation of IDF curves under climate change scenarios in Canada. WEBSE_{IDF} was developed in three stages: (1) collection of the rainfall intensity measurements database; (2) construction of IDF curves and mathematical models; and (3) development of a web-based GIS interface allowing simple browsing by users.

2.7.1. Consolidation of a Rainfall Intensity Database

To determine maximum rainfall intensities for durations between 1 and 24 h from pluviograph gauges, data from pluviograph strip charts must be analyzed (see details in [61]). However, there are limits to the usefulness of these data for durations of less than one hour. To overcome this

problem, a device that uses an algorithm for automatic digitization of pluviograph strip charts was developed to calculate rainfall intensities for 15-min increments, ranging from 0.25 to 24 h (see details in Section 2.7.2). The device significantly improves the reading resolution of rainfall intensity records for the construction of IDF curves in Chile. It was initially used to estimate the rainfall intensity signals from the pluviograph strip charts kept by the National Directorate of Water Resources (DGA), the government organization responsible for monitoring and managing water resources in Chile. Additionally, data were digitized from pluviograph strip charts maintained by other water-related institutions, such as the Chilean Meteorological Directorate and the electric generation company ENEL (also known as ENDESA). After all data from the collected strip charts were digitized, a database containing 47 pluviograph gauges (see Appendix A) was consolidated, containing at least 15 years of rainfall intensity records. The established threshold allowed for the development of a database that can be considered statistically reliable, relative to the historical pluviograph records available in the country. Regarding the length of the rainfall series, it is important to mention that at least 30 years of records are needed to reduce the uncertainty of the rainfall estimates for T greater than 20 years. This is an advantage of $WEBSE_{IDF}$ because it allows the users to make updates in the spatio-temporal resolution of the database, that is, increase the number of gauges or add new records in existing gauges.

2.7.2. Pluviograph Strip Charts Reader

A device named a pluviograph strip charts reader (PSCR) was developed to digitize the analog pluviograph strip charts (manuscript under preparation). The PCSR significantly reduced the time to analyze a single pluviograph strip chart, because traditional time-consuming and error-prone manual techniques are replaced by a semi-automatic process of tracing the rainfall signal. The device was designed to read rainfall intensities in increments as small as 15 min, with a temporal displacement of 5 min; thus, the PCSR can generate a whole range of rainfall intensity durations. However, because of the thickness of the drawn trace in the pluviograph strip charts, rainfall intensity for durations of less than 15 min cannot be reliably extracted. In fact, reading tests show unreliable intensity readings at resolutions lower than 15 min. As a result, $WEBSE_{IDF}$ was implemented to provide the following durations: 0.25, 0.5, 0.75, 1, 2, 4, 8, 12, and 24 h. The configuration of PSCR has the following components: (1) processing server, (2) scanner, and (3) digitization software (Figure 1).

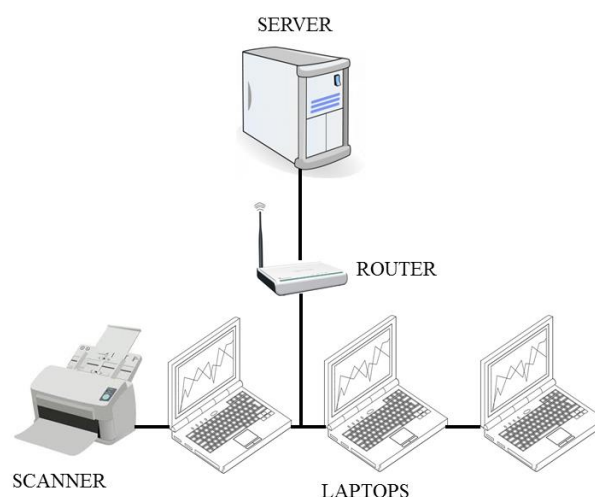


Figure 1. Main components of the pluviograph strip charts reader (PSCR).

The software used in PSCR is web-based and server-stored. It enables the simultaneous analysis of pluviograph strip charts via wireless connection, for up to five end users, without affecting the computational efficiency. This capability means a considerable reduction in processing time, as well as an increased capacity for extracting and managing large volumes of data. The PSCR uses a

scanner to extract the rainfall intensity data, taking into consideration the need to acquire images from pluviograph bands of the size 9×42.5 cm. The scanner is an Epson Workforce Pro GT-S50, with automatic sheet feeder, able to read 50 double-sided sheets per minute. Given the size of the charts, the scanner was configured to capture images at a resolution of 5019×1181 pixels and 300 dots per inch (dpi).

Using the algorithm designed for the automatic digitization of strip charts, the PSCR automatically generates a trace of the rainfall intensity signal that is overlaid on the scanned image. This trace can be adjusted by the end user to correct possible errors derived from handwritten annotations, which are very common and can reduce the effectiveness of the algorithm. Once the band trace has been completed, rainfall intensity time series can be extracted as a plain text file, which can then be used to calculate annual maximum rainfall intensities. As a validation procedure, the digitized rainfall intensity data obtained from PSCR for durations of 1, 6, and 24 h were compared to manually extracted data for the same durations. For all analyzed cases, the Mann–Whitney U test confirmed that there were no statistically significant differences (α -level or significance level of 0.05) in the calculated values of rainfall intensity.

2.7.3. Database for Mathematical Models

Each of the mathematical models was developed in Python using the methods described in Section 2.4, and then implemented in WEBSE_{IDF}. The modelling process is conducted in two stages: (1) a PDF (see Table 1) is fitted to the annual maximum rainfall intensities associated with each duration (D) and return period (T), and (2) an analysis using ordinary least squares regression (OLSR) was conducted to estimate the optimal parameters for all the models presented in Table 2 [62]. The performance of the models is evaluated using the tests described in Table 3. Additionally, a geostatistical tool that uses ordinary Kriging [63] was also built-in to perform spatial interpolations and create isolines of maximum rainfall intensities within central Chile.

2.7.4. Informatic Development of WEBSE_{IDF}

The development of WEBSE_{IDF} responded to the need of an easily accessed database for rainfall intensity data extracted from pluviograph strip charts. In fact, WEBSE_{IDF} is the first web-based system for IDF curves in Chile, and there are no similar systems available. WEBSE_{IDF} is an innovative tool for storing, visualizing, and analyzing rainfall intensity data. The system required the addition of a spatial support component; PostGIS, which is an extension of the popular PostgreSQL, was used. A PHP (hypertext preprocessor) was used to connect directly to the database to visualize, modify, and register data supplied by the user and the stations that contain information about maximum rainfall intensities. A connection between Python and the database was established so that all mathematical operations and statistical analyses described in Sections 2 and 2.1–2.6 could be performed. The libraries NumPy, SciPy, and Matplotlib were used. The results of the calculations were formatted using JSON, read using JavaScript, and finally visualized on a web page using HTML (v4). JavaScript libraries such as Flot were used to visualize the IDF curves. To generate the equations related to the IDF curves, LaTeX and MathML were used by the libraries JQuery and MathJax. For the graphical user interface (GUI), the Mapserver tool was used to create map visualizations displaying the available pluviograph gauges and rain gauges. Finally, WEBSE_{IDF} was developed for common browsers including Internet Explorer, Mozilla Firefox, and Google Chrome (see Figure 2 for details). All software and informatics steps performed to develop WEBSE_{IDF} are similar to those used by the authors of [23], in the development of a web-based tool for IDF curves estimation under climate change scenarios in Canada.

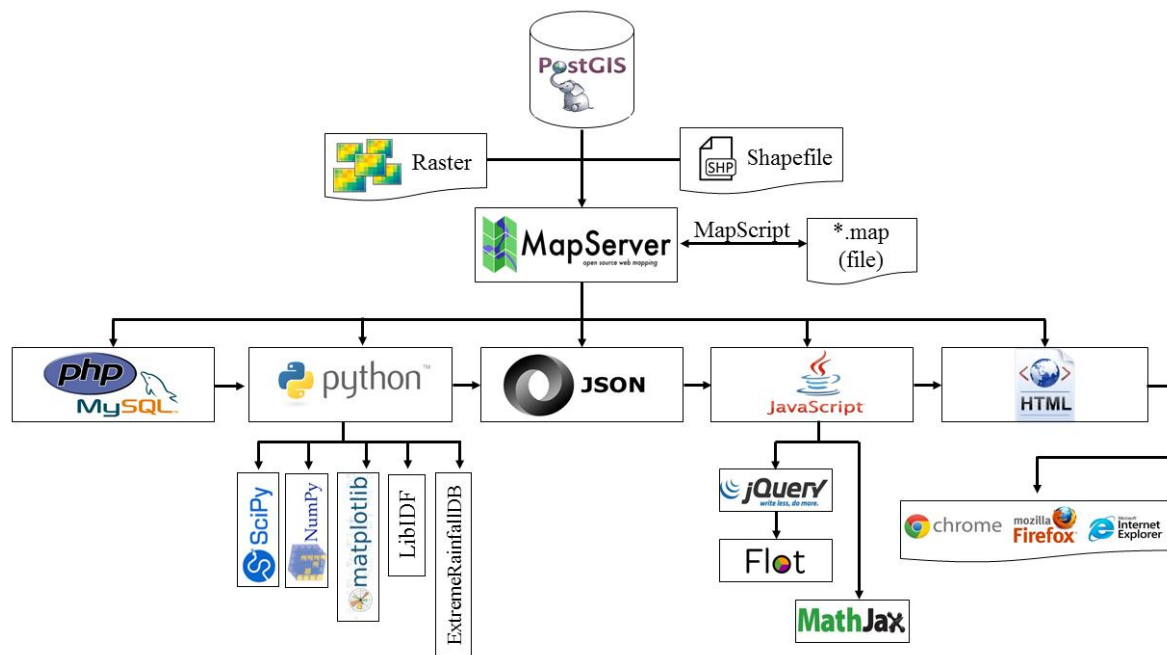


Figure 2. Informatic structure of web-based system for the estimation of intensity–duration–frequency (IDF) curves (WEBSE_{IDF}). GIS—geographical information system.

Some of the important advantages of WEBSE_{IDF} are the following:

1. The system is web-based, allowing users to access it from any location with an Internet connection.
2. Its GIS-based architecture allows the integration of hardware, software, and georeferenced data in the process of capture, storage, manipulation, analysis, and visualization.
3. Its flexibility allows users to easily incorporate additional spatial data into the system—that is, the database allows the addition of new pluviograph gauges.
4. It is flexible enough to incorporate new processing algorithms and models to represent IDF curves.

The architecture and functionality of WEBSE_{IDF}, which are linked to a GIS component, require the integration of different programming languages—that is, those used for mathematical calculations, and those used for management of the database. This system is designed to enable continuous development and improvement, to ensure current and future relevance to the management of water resources in central Chile.

2.7.5. Georeferenced Database

The georeferenced database (geodatabase) for WEBSE_{IDF} was designed to store, organize, and manipulate rainfall intensity data. The geodatabase design accounted for the following entities: (1) *Users*, which contains the list of users registered in the system; (2) *Station*, which stores the data from each pluviograph gauge or rain gauge; (3) *User_Station*, which stores the user's data related to station data; (4) *Maximum_Yearly_Precipitation*, which contains the precipitation data from the pluviograph gauges or rain gauges; and (5) *Users_Maximum_Yearly_Precipitation*, which is a copy of the data provided in (4), allowing each user to have their own copy of the data (see Figure 3 for details).

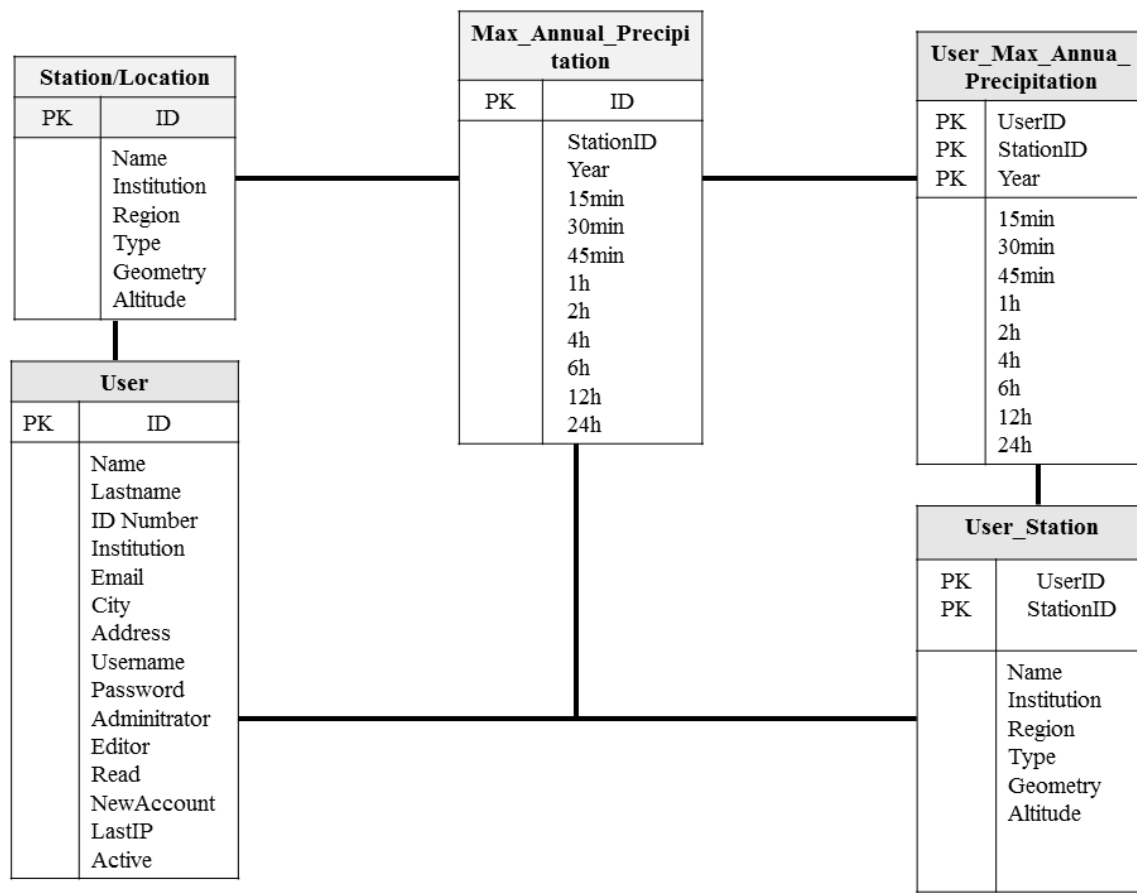


Figure 3. Geodatabase included in WEBSE_{IDF}. PK refers to Primary Key Fields that link the ID across different tables.

2.7.6. Graphical User's Interface (GUI) of WEBSE_{IDF}

The WEBSE_{IDF} interface has an intuitive structure that allows users to easily explore all the tools available in the system. In fact, the GUI (graphical user interface) enables users to interact with available data and to generate the visualization of IDF curves and their mathematical models. The structure of the interface (Figure 4) is composed of the following elements: (a) a geographical information system (GIS) with a drop-down menu that contains satellite maps, cartographic information—that is, water resources, road networks, administrative divisions, and so on; (b) a georeferenced pluviographic and pluviometric gauges; (c) a toolbar menu that the user can use to manipulate the visualization in the GIS environment; and a control panel that allows administrative control of access privileges.

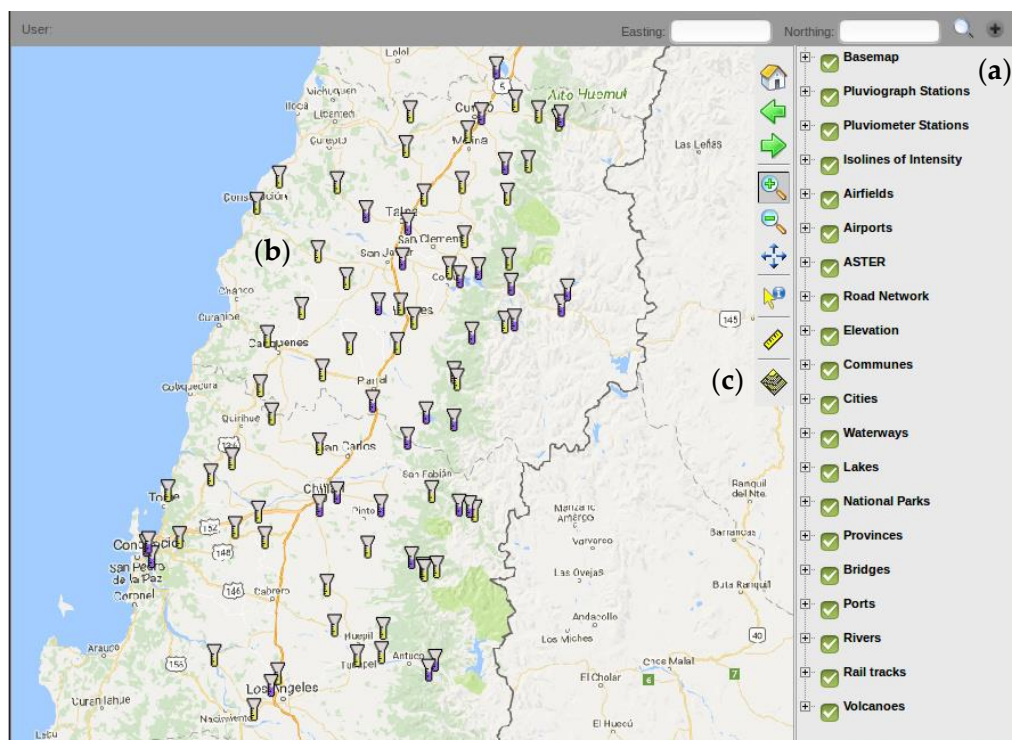


Figure 4. Graphical user's interface of WEBSE_{IDF}. (a) Drop-down menu; (b) georeferenced pluviograph and pluviometric gauges; and (c) toolbar menu.

2.7.7. Procedure to Generate IDF Curves Using WEBSE_{IDF}

The generation of IDF curves in WEBSE_{IDF} is a straightforward procedure. First, a user account must be created, a process described in Section 3.1. WEBSE_{IDF} contains a point-based database for central Chile that can be accessed, extracted, modified, and analyzed. This database has pluviograph and pluviometric gauges that can be used to generate IDF curves. For ungauged areas, the ordinary Kriging interpolation method allows for the construction of IDF curves at any spatial location within central Chile. In pluviometric gauges (24-h rainfall accumulation), the SI method is used to generate the IDF curves. Users can select from a complete set of PDFs, estimation methods, and IDF models to analyze and compare the sensitivity of the generated IDF curves. The flexibility of WEBSE_{IDF} allows users to save modifications made to the database without affecting the records contained in the original database. This option is very useful for generating climate change scenarios based on modified rainfall intensity records [23]. These steps are summarized in Figure 5.

2.7.8. Considerations about the Methodologies Included in WEBSE_{IDF}

The selection and compilation of storm records can include PDS or AMS. In general, PDS for frequency analysis can generate higher values for a given frequency, compared with AMS. The difference in rainfall intensity values is generally greater for the most frequent events (i.e., 2-year, 5-year, 10-year), and it decreases as the return period increases, that is, the difference in rainfall intensity values is minimal for less frequent events (i.e., 25-year, 50-year, 100-year, 500-year). The selection of either PDS or AMS can have significant implications in the design or control of drainage and flood prevention infrastructures [64,65]. Accordingly, it is recommended to test both types of series (with different PDFs and IDF models) to select the most appropriate model for the management of extreme hydrological events.

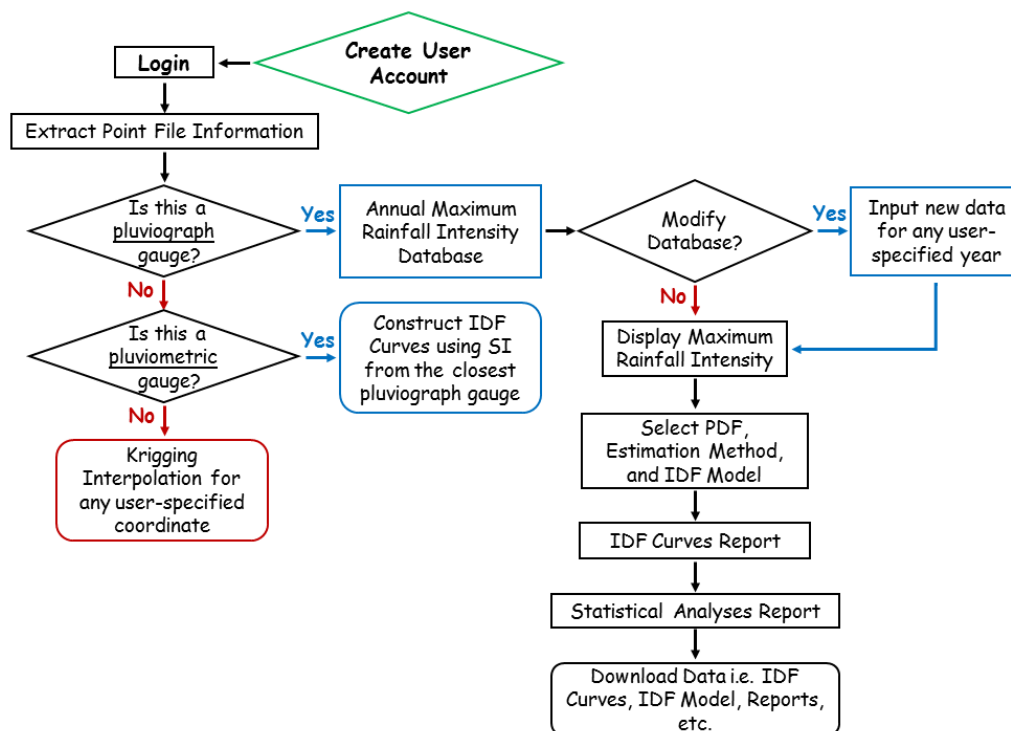


Figure 5. Flow diagram showing the general procedure to generate IDF Curves in WEBSE_{IDF}. S_I—storm index; PDF—probability distribution function.

Regarding the ordinary Kriging method of interpolation included in WEBSE_{IDF}, it is worth mentioning that this is just one of many techniques that can be used for the interpolation of spatial data. The basic assumption of Kriging is the principle that data spatially closer are more likely to be more similar in behavior than data with a larger separation distance. Although this assumption largely holds for climate data, there are other factors that determine rainfall intensities such as elevation and proximity to large bodies of water. Although techniques such as co-Kriging or regression Kriging can be used to model secondary variables, the ordinary Kriging method implemented in the WEBSE_{IDF} system does not take this data into account, although currently, active research is being carried out to determine how best to model these and other secondary variables. Furthermore, another simplification introduced into the WEBSE_{IDF} system is that users cannot estimate the covariance structure of the data. The covariance structure of the rainfall data was previously analyzed and determined and hence the covariance parameters have been fixed. As many users of the system may not be familiar with geostatistical methods and the associated parameter estimation stage, it was decided to fix these, which also ensures the stability of the Kriging process. When adding data from other spatial locations where rainfall characteristics maybe significantly different to the target area in south-central Chile, it will be necessary to reestimate these parameters.

3. Results and Discussion

3.1. Register, Login, and Use of WEBSE_{IDF}

WEBSE_{IDF} is currently hosted on a server at the University of Talca, and can be accessed through the following link: <http://ree.ctha.cl> (or <http://see.otalca.cl> for spanish version). The system is able to store information from the end users to facilitate analysis about its usage. The conditions about usage and privacy policies have been established according to confidentiality policies. Once a user's account has been created, their username and password are directed to a new window (Figure 6a) where it is possible to login into WEBSE_{IDF}. In the next window, users can either start a new session or continue

from a previous saved session, allowing them to make changes to the database and save these changes for future use (Figure 6b).

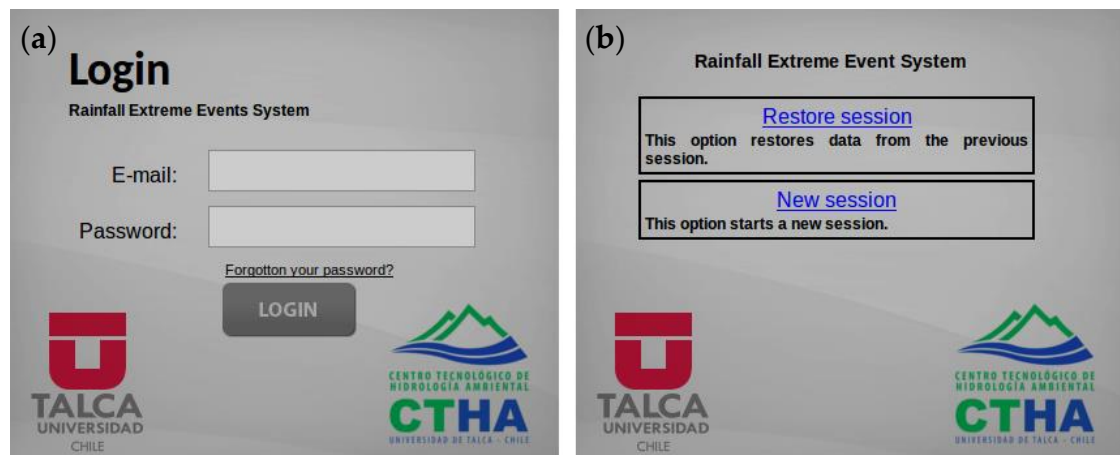


Figure 6. Graphical user interface (GUI) for the creation of new a user account in WEBSE_{IDF}.

(a) The login screen, (b) Restore previous session option.

3.2. Spatial Visualization and Adding New Data into WEBSE_{IDF}

To visualize or analyze rainfall intensity data in WEBSE_{IDF}, users can generate queries by selecting a point-based feature (pluviograph gauge or rain gauge), or by entering the coordinates of the area of interest within central Chile (all available point-based features would be included inside this polygonal domain). For instance, if the user selects a single pluviographic gauge or pluviometric gauge (rain gauge), or clicks on the map, a new window providing specific information about the selected feature(s) opens up. The menu for this window allows selection of the PDF, the parameter estimation method, and the IDF model for each selected pluviographic gauge or pluviometric gauge. Once this information is selected, the user can visualize and export the following data and results: (1) annual maximum precipitation accumulation for different durations; (2) annual maximum rainfall intensity for different durations; (3) IDF curves; (4) mathematical models; (5) storm index; (6) statistics; (7) export; and (8) other associated analysis (Figure 7).



Figure 7. Visualization and analysis of rainfall intensity for a pluviographic gauge (San Javier) included in WEBSE_{IDF}.

For any pluviographic gauge or rain gauge, it is possible to add new data—that is, information on maximum storm precipitation accumulation from newly acquired years. These data must be inputted for the entire range of durations established in `WEBSEIDF`, that is, 0.25, 0.5, 0.75, 1, 2, 4, 8, 12, and 24 h (see Figure 8), by an operator. Administrative privileges are required for users to be able to add new data to `WEBSEIDF`.

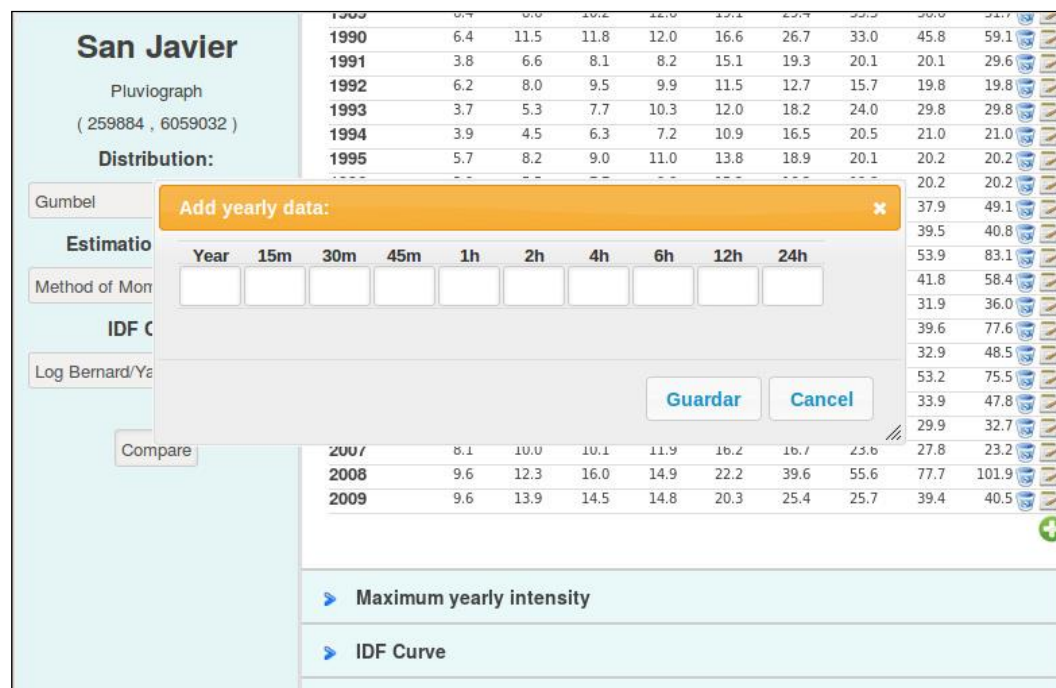


Figure 8. Tabular form of precipitation accumulation data from a pluviograph gauge (San Javier) included in WEBSE_{IDF}. New precipitation accumulation data for different durations can be inserted, as shown.

3.3. Graphical Visualization of IDF Curves

The annual maximum rainfall accumulation for a selected pluviograph gauge or rain gauge is converted into annual maximum intensities for the whole range of durations established in $WEBSE_{IDF}$. This conversion provides data suitable for the estimation of IDF curves. In the current version of $WEBSE_{IDF}$, the users can select any of the three available PDFs, the method for parameter estimation, and the IDF model to be fitted using the original rainfall intensity data. After selecting this primary information, the user can obtain a graphic representation of the IDF curves and the selected IDF model with its corresponding parameter values. The system allows positioning the mouse over any IDF curve to get a pop-up window showing the intensity of rainfall, the duration, and the corresponding return period. This is a handy option to easily display and determine rainfall intensity values along the IDF curves (see Figure 9). To determine the best fit for combinations of selected PDF and IDF models, the results of the fitted PDFs and mathematical models can be displayed in the Statistics module, which provides the results of three goodness of fit tests included in $WEBSE_{IDF}$: Mann–Whitney, Kolmogorov–Smirnov, and coefficient of determination (see Section 2.5 and Figure 10 for details).

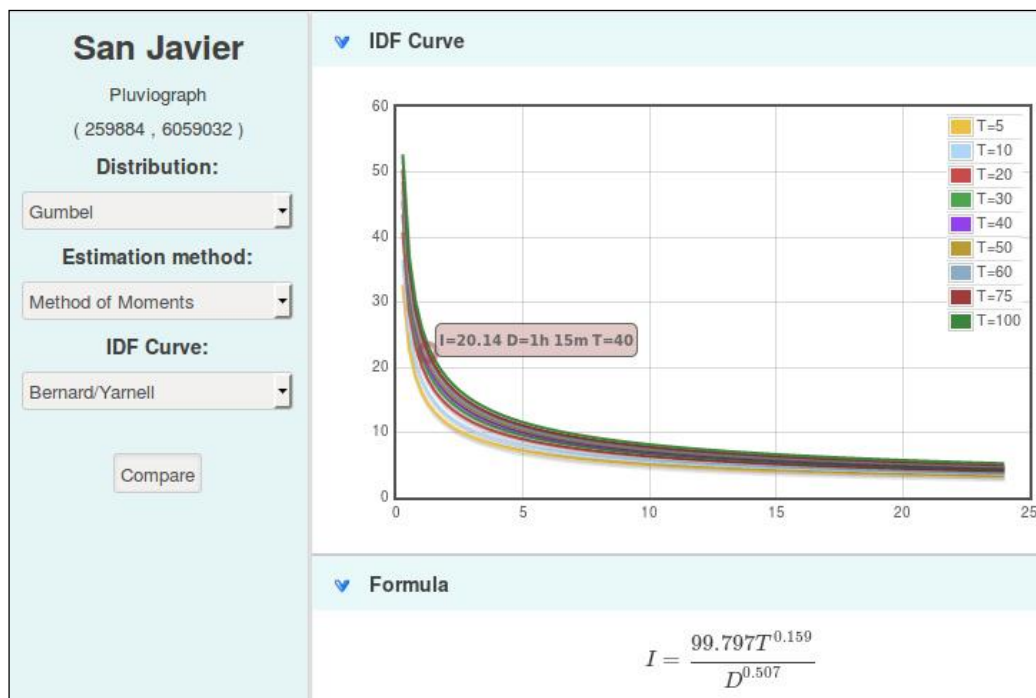


Figure 9. Graphic visualization of IDF curves and IDF model for a pluviograph gauge (San Javier City) included in WEBSE_{IDF}.

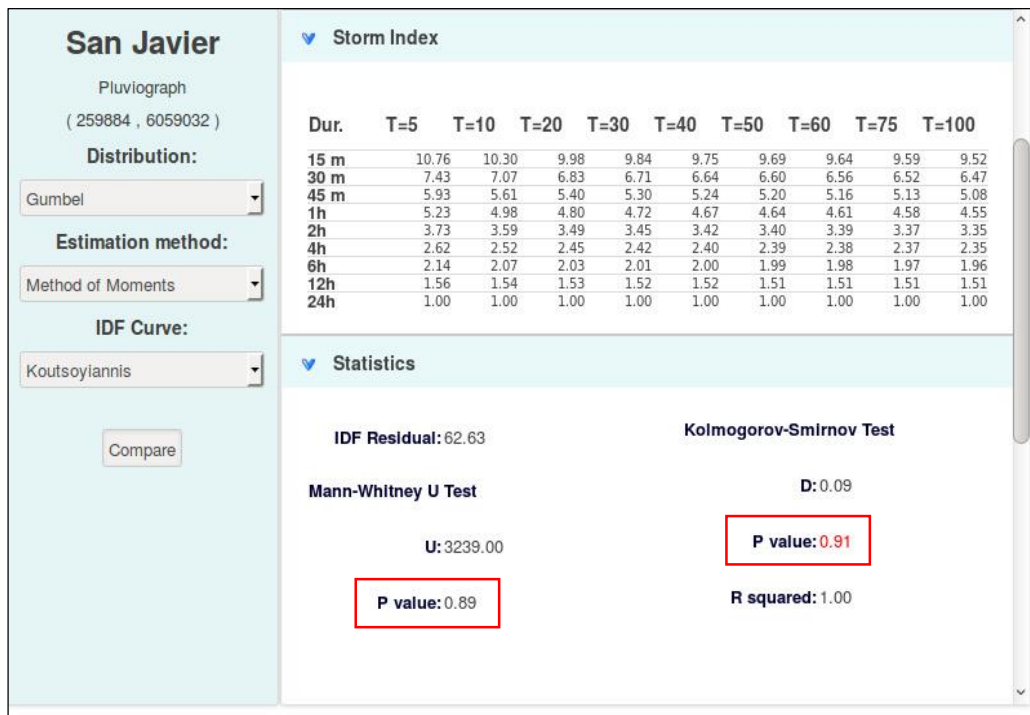


Figure 10. Storm index (S_I) calculated for each duration and return period of a pluviographic gauge (Talca City) included in WEBSE_{IDF}. The results of the goodness of fit represent the modeled rainfall intensity, because of the combination between any selected PDF and IDF model. As the p values in the red boxes are larger than the α -level ($\alpha = 0.1$), the Gumbel PDF is accepted for San Javier.

3.4. Extrapolation of IDF Curves

To extend the spatial distribution of IDF curves to pluviometric gauges (24-h rainfall accumulation), the storm index (S_I) method [32] was implemented in WEBSE_{IDF}. Users can construct IDF curves for the pluviometric gauges using the S_I of a reference pluviograph gauge. As a reasonable rule of thumb, Pizarro et al. (2015) [32] suggested that consistent extrapolations of IDF curves are attained when the maximum absolute difference between the raw rainfall intensity in 24 h for both pluviographic and pluviometric gauges does not exceed 2 mm/h. In WEBSE_{IDF} the S_I is first calculated in a reference pluviographic gauge, and then used to generate IDF curves, their mathematical models, and statistics of interest for any neighboring pluviometric gauge. WEBSE_{IDF} also allows the users to download .xls and .pdf formats of the raw data and IDF curves. More details about the options available in WEBSE_{IDF} can be obtained from the user's manual.

3.5. Geostatistical Interpolation of IDF Curves

Geostatistical interpolation of maximum rainfall intensities at specific user-defined locations is also available in WEBSE_{IDF}. The system uses ordinary Kriging interpolation to reproduce a spatial prediction of IDF curves at any location of interest within central Chile. Available in the main interface toolbar, the interpolation option can be applied by selecting any spatial location or geographic point where the IDF curves need to be interpolated (Figure 11). The interpolation can be also applied for any selected pluviographic or pluviometric gauge. Once the user selects a point of interest (gauge), a report is displayed indicating the coordinates of the selected location, and the distance in kilometers from the nearest pluviograph and pluviometric gauges.

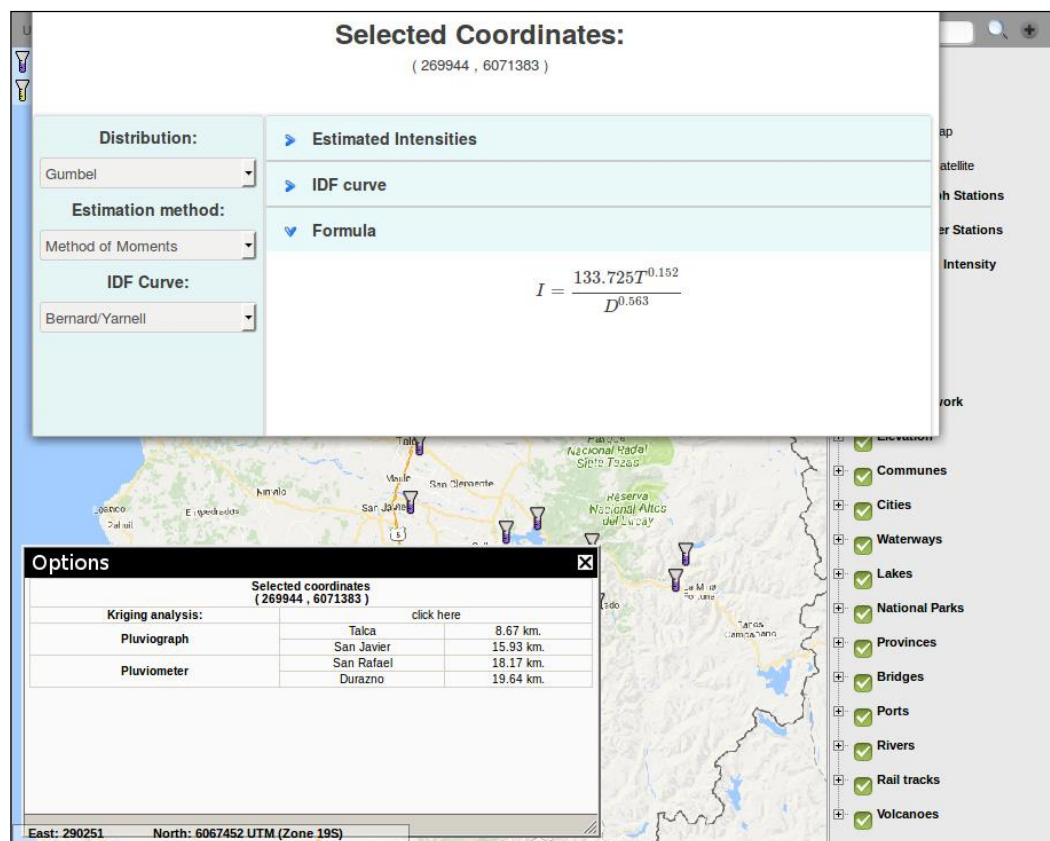


Figure 11. Geostatistical interpolation of IDF Curves in WEBSE_{IDF} using ordinary Kriging method at a selected location.

3.6. Isolines of Maximum Rainfall Intensity

This option allows generating isolines for the maximum rainfall intensity, considering all the pluviographic and pluviometric records available in central Chile. This choice can be accessed from WEBSE_{IDF} drop-down menu. Activating this preference deploys isolines in the map for any selected duration and return period (Figure 12a,b). The rainfall intensity value (mm/h) contained in the isolines map can be displayed by positioning the identification tool (from the toolbar menu) over any desired spatial location. This selection allows for the visualization of the spatial distribution of maximum rainfall intensity records in central Chile, and the differences associated with the whole range of durations and return periods. The isolines of maximum rainfall intensity for any duration and return period are plotted considering all the available records available in WEBSE_{IDF} database. The rainfall intensity value of any selected isoline is automatically displayed in a new window (see Figure 12).

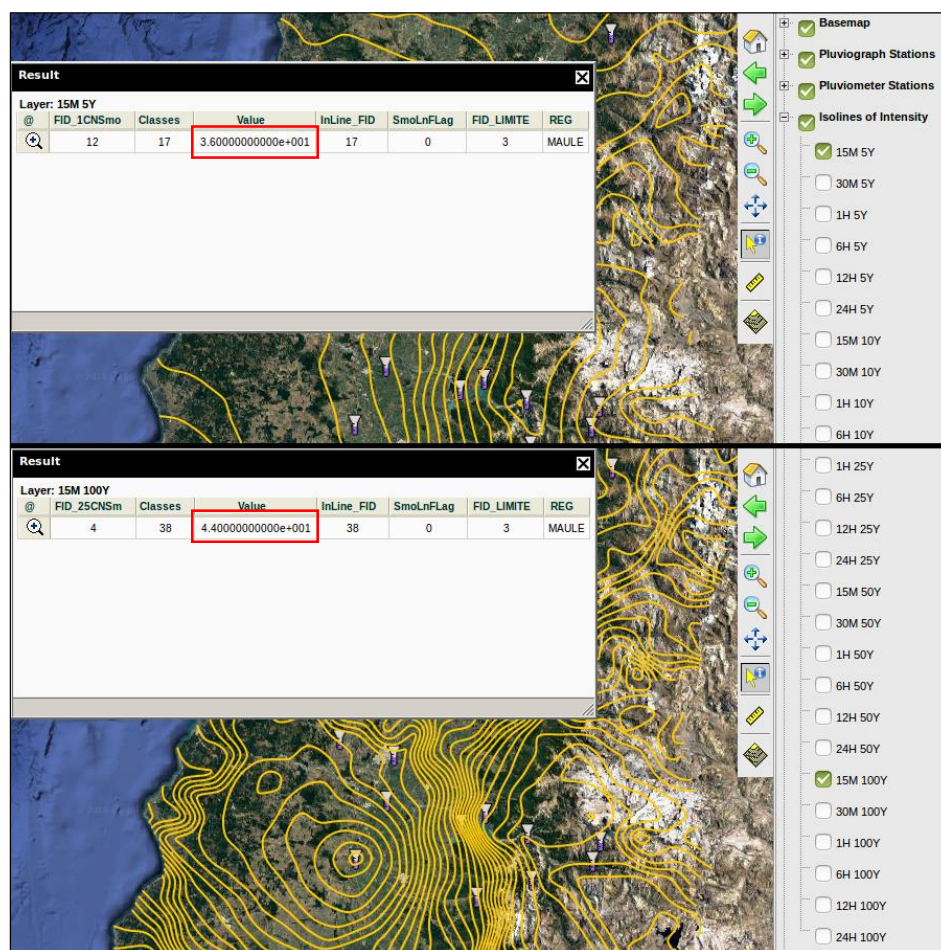


Figure 12. Isolines of maximum rainfall intensity for D = 15 minutes associated with (a) T = 5 years; and with (b) T = 100 years in WEBSE_{IDF} using ordinary Kriging interpolation. The interpolated value for each frequency is shown in the red boxes.

4. Conclusions

WEBSE_{IDF} is a web-based system that has been developed to consolidate a database of historical rainfall intensity records for central Chile. The system stores, visualizes, and analyzes maximum rainfall intensity records between 15 min and 24 h from pluviographic or pluviometric gauges, to generate IDF curves at any spatial location within the domain of central Chile. This is the first system capable of generating this level of spatio-temporal resolution in the development of IDF curves in central Chile. This innovation is very important because extreme rainfall events of shorter durations

have often proven to be more powerful and destructive than those of longer duration. Additionally, the IDF curves can be extrapolated to ungauged areas (i.e., pluviometric gauges) using rainfall intensity data from pluviographs combined with the S_I scaling method. $WEBSE_{IDF}$ also makes it possible to generate IDF curves for ungauged areas by interpolating data of existent pluviograph gauges. This approach to generate IDF curves has a substantial advantage, compared with methodologies such as generalized IDF curves, because it allows for the disaggregation of data on the spatial variability of rainfall intensity to a higher spatial resolution. Finally, it is important to point out that one of the major advantages of $WEBSE_{IDF}$ is the flexibility that allow users to add new rainfall intensity records into the database. $WEBSE_{IDF}$ is freely available for students, researchers, and other relevant professionals, providing capabilities that can be used to improve technical decisions of public and private institutions. The database provided by $WEBSE_{IDF}$ can be used in the design of major and minor storm water management systems, sanitary sewers, retention ponds, culverts, bridges, dams, pumping stations, roads, and drainage planning, and so on, to mitigate the impacts of extreme events in central Chile.

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Abbreviations

| | |
|---------------|---|
| IDF | Intensity–Duration–Frequency Curves |
| $WEBSE_{IDF}$ | Web-based System for the Estimation of IDF Curves |
| S_I | Storm Index Method |
| PD | Probability Density Function |
| CD | Cumulative Distribution Function |
| AM | Annual Maximum Series |
| PD | Partial Duration Series |
| T | Return Period |
| D | Storm Duration |
| GEV | Generalized Extreme Value |
| MoM | Method of Moments |
| ML | Maximum Likelihood Method |
| PWM | Probability Weighted Moments |
| K–S test | Kolmogorov–Smirnov Test |
| IDW | Inverse Distance Weighting |
| PSCR | Pluviograph Strip Charts Reader |
| DGA | Dirección General de Aguas |
| ENEL | Enel Distribución Chile S.A. |
| DMC | Dirección Meteorológica de Chile |

Appendix A

Table A1. Pluviograph gauges included in WEBSE_{IDF}. The pluviographs bands were contributed by three Intitutions: The National Directorate of Water Resources (DGA), The National Company of Electricity (ENEL), and the National Meteorological Directorate (DMC).

| Origin | Name | Lat (S) | Long (W) | Period of Records | Available Years |
|--------|----------------------------|---------|----------|-------------------|-----------------|
| DGA | Embalse Rungue | 33°01' | 70°55' | 1979–2007 | 26 |
| DGA | Cerro Calán | 33°23' | 70°32' | 1975–2012 | 38 |
| DGA | Los Panguiles | 33°26' | 71°00' | 1981–2011 | 31 |
| DGA | Pirque | 33°40' | 70°36' | 1972–2010 | 39 |
| DGA | Melipilla | 33°40' | 71°11' | 1975–2012 | 37 |
| DGA | La Obra | 33°35' | 70°29' | 1995–2012 | 18 |
| DGA | Huechun Andina | 33°04' | 70°46' | 1994–2012 | 15 |
| DGA | San Antonio | 33°34' | 71°37' | 1997–2011 | 15 |
| DGA | MOP-DGA | 33°26' | 70°38' | 1992–2008 | 17 |
| DMC | Tobalaba | 33°27' | 70°32' | 1998–2009 | 12 |
| ENEL | Quinta Normal | 33°26' | 70°40' | 1917–2009 | 89 |
| ENEL | Cerrillos | 33°29' | 70°42' | 1960–2005 | 45 |
| ENEL | Pudahuel DMC | 33°23' | 70°47' | 1974–2009 | 36 |
| ENEL | Edificio Central Endesa | 33°27' | 70°39' | 1969–2001 | 23 |
| DGA | Los Queñes | 35°00' | 70°49' | 1974–2009 | 36 |
| DGA | Potrero Grande | 35°12' | 71°07' | 1971–2009 | 38 |
| DGA | Pencahue | 35°23' | 71°48' | 1974–2009 | 36 |
| DGA | Talca | 35°26' | 71°35' | 1982–2009 | 28 |
| DGA | San Javier | 35°36' | 71°44' | 1974–2009 | 36 |
| DGA | Colorado | 35°38' | 71°16' | 1969–2009 | 40 |
| DGA | Melozal | 35°45' | 71°47' | 1971–2009 | 35 |
| DGA | Embalse Ancoa | 35°54' | 71°17' | 1971–2009 | 38 |
| DGA | Parral | 36°09' | 71°50' | 1974–2009 | 36 |
| DGA | Embalse Digua | 36°15' | 71°32' | 1971–2009 | 39 |
| DGA | Embalse Bullileo | 36°17' | 71°26' | 1971–2009 | 39 |
| DGA | San Manuel | 36°21' | 71°39' | 1995–2009 | 15 |
| DMC | Curico | 34°57' | 71°13' | 1966–2009 | 40 |
| ENEL | Armerillo | 35°42' | 71°06' | 1959–2000 | 41 |
| ENEL | Casa de Maq. Cipreses | 35°48' | 70°49' | 1964–2000 | 30 |
| ENEL | Desague Laguna Invernada | 35°44' | 70°47' | 1963–1980 | 18 |
| ENEL | Melado en la Lancha | 35°51' | 71°04' | 1966–1993 | 25 |
| ENEL | El Lirio | 35°40' | 71°21' | 1968–1994 | 27 |
| DGA | Embalse Coihueco | 36°35' | 71°47' | 1971–2009 | 38 |
| DGA | Chillán Viejo | 36°38' | 72°08' | 1974–2009 | 36 |
| DGA | Embalse Diguillín | 36°50' | 71°44' | 1965–2009 | 45 |
| DGA | Quilaco | 37°41' | 72°00' | 1965–2009 | 45 |
| DGA | Cerro El Padre | 37°46' | 71°53' | 1970–2009 | 40 |
| DGA | Caracol | 36°38' | 71°23' | 1987–2009 | 23 |
| DGA | Contulmo | 38°00' | 73°13' | 1987–2009 | 21 |
| DGA | La Punilla | 36°39' | 71°19' | 1965–1986 | 20 |
| DMC | Chillan | 33°35' | 72°02' | 1974–2009 | 30 |
| DMC | Concepcion, Carriel Sur | 36°46' | 73°3' | 1966–2009 | 44 |
| DMC | Concepcion, Bellavista | 36°49' | 73°02' | 1965–1988 | 22 |
| DMC | Concepcion, Hualpencillo | 36°46' | 73°03' | 1946–1963 | 13 |
| DMC | Los Angeles, Maria Dolores | 37°24' | 72°25' | 1995–2009 | 15 |
| ENEL | Polcura en Balseadero | 37°19' | 71°32' | 1959–2000 | 40 |
| ENEL | Troyo | 38°14' | 71°18' | 1968–1994 | 27 |

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